

**Abbreviations**

AIISI	American Iron and Steel Institute
ALBs	Airlift bioreactors
CMC	Sodium salt of carboxymethyl cellulose
SRILAB	Split-rectangle-internal loop airlift bioreactor
NuT	Newcastle-upon-Tyne tap water

**Nomenclature**

$a$	Gas/liquid interface area ( $\text{m}^2 \text{m}^{-3}$ )
$A_d/A_r^{1.618}$	Downcomer to riser area partition following the golden ratio
$A_r/A_d^{1.618}$	Riser to downcomer area partition following the golden ratio
$C^*$	Concentration of oxygen at saturation ( $\sim 8.1 \times 10^{-3} \text{ kg m}^{-3}$ @ 25 °C and 1 atm)
$C_L$	Actual dissolved oxygen concentration measured at regular intervals ( $\text{kg m}^{-3}$ )
$C_x$	Coefficient in Equation 4
DO	Dissolved oxygen concentration ( $\text{kg m}^{-3}$ )
$h$	Height (m)
$k_L$	Oxygen transfer coefficient ( $\text{m s}^{-1}$ )
$k_{La}$	Overall oxygen transfer coefficient ( $\text{s}^{-1}$ )
$n$	Exponent in Equation 4
$\emptyset$	Diameter (m)
SQ	Square cross section ( $\text{m}^2$ )
$t_M$	Mixing time (s)
$U_G$	Linear gas velocity ( $\text{m s}^{-1}$ )
$U_L$	Linear velocity of the liquid ( $\text{m s}^{-1}$ )
$V_f$	Final volumes ( $\text{m}^3$ )
$V_i$	Initial volumes ( $\text{m}^3$ )
vvm	Volume per volume per minute ( $\text{m}^3 \text{min}^{-1}$ )

**Greek letters**

$\varepsilon_g$	Gas holdup (-)
$\varepsilon$	Gas holdup in Equation 4
$\mu$	Dynamic viscosity ( $\text{mPa}\cdot\text{s}$ @ 25 °C)
$\phi$	Golden ratio $[(1+\sqrt{5})/2 = 1.618]$

**Hydrodynamics of split-rectangle-internal loop airlift bioreactor with variations in riser and downcomer cross-sectional areas based on the golden ratio**

**Short title:** Golden ratio and airlift bioreactors

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**Keywords:** Airlift bioreactor; Golden ratio, Hydrodynamic performance.

## ABSTRACT

**Background:** The use of bioreactors that mimic industrial reality is essential if knowledge transfer is desired. This is particularly important once filamentous microbes face harsh conditions hindering the formation of biofilms in some types of bioreactors and thus diminishing their ability to perform biotransformation or production of secondary metabolites. Airlift bioreactors can circumvent such problems; however, the lack of consensus regarding riser and downcomer partition persists. The use of golden ratio is a possibility to be considered. Our proposition was to evaluate the hydrodynamic performance and mass transfer in split-rectangle-internal loop airlift bioreactors using golden ration partition. **Results:** In a general way, results revealed that a partition of  $A_r/A_d^{1.618}$  presents better and more desirable characteristics than  $A_d/A_r^{1.618}$  for linear liquid velocity ( $U_L$ ), mixing time ( $t_M$ ), gas holdup ( $\epsilon_G$ ), ~~liquid pressure ( $P_L$ )~~, and volumetric oxygen transfer coefficient ( $k_{La}$ ). Such behavior was observed even when the SRILAB operated under different linear gas velocities ( $U_G$ ) regimens (0.5 to 1.5 vvm) and Newtonian and non-Newtonian bulk fluids. **Conclusion:** Such results support the idea of using golden ratio as riser-to-downcomer partitioning parameter in airlift bioreactors.

Key words: airlift bioreactors, golden ratio, downcomer-to-riser, hydrodynamics.

## 1 INTRODUCTION

2 Stirred tank bioreactors are not the best options for bioprocesses involving fungi  
3 and other filamentous organisms due to high shear rates generated that compromise the  
4 morphology and/or integrity of submerged cells.<sup>1</sup> In this context, ~~airlift-bioreactors~~ ALBs  
5 present a valuable resource for fungal growth, even as biofilm phenotype. Other  
6 advantages of ALBs include their simple design with no moving parts or agitator, easier  
7 sterilization, lower energy requirement, and greater heat-removal.<sup>2</sup>

8 Regarding hydrodynamics, ~~variations in cross-sectional areas of riser and~~  
9 ~~downcomer ( $A_r/A_d$  and  $A_d/A_r$ ) are amongst~~ the more critical parameters. Different authors  
10 report varying results in terms of the performance and ~~cross-sectional area~~ ratios;  
11 however, without any consensus. Most operated concentric draft tubes or external loop  
12 ALBs,<sup>3-7</sup> in which is more difficult to set different geometries.

13 To our knowledge, none has ~~proposed~~ using the golden ratio [ $\phi = (1+\sqrt{5})/2 = 1.618$ ]  
14 ~~as parameter for  $A_r/A_d$  or  $A_d/A_r$  settings~~, even with sufficient evidence that it may be  
15 advantageous for fluidic systems. ~~Different authors have shown that such proportion~~  
16 ~~improves fluid mixing and should be considered for liquid systems.~~<sup>8-12</sup>

17 The aim of this study is to evaluate the ~~impact on~~ hydrodynamic performance when  
18 golden ratio is used ~~as a criterion for cross-sectional areas~~ partitioning.

## 20 MATERIALS AND METHODS

### 21 Bioreactor conception and design

22 One SRILAB (Figure 1A) was constructed in AISI304 stainless steel, with 0.002 m  
23 wall thickness and SQ of 0.10 m and h of 0.70 m. A flanged expansion chamber  
24 (degassing zone) of 0.25 m (SQ) × 0.15 m (h) was welded onto this column. A 0.09 ×  
25 0.025 m silicon mattress with 50 holes of 0.0005 m  $\phi$  placed at the bottom of the column  
26 acted as gas sparger. The SRILAB had a working volume of 0.012 m<sup>3</sup>.

A movable AISI304 stainless steel partition baffle of  $0.65 \times 0.096$  mm was placed inside the column to create riser and downcomer environments. It generated a geometric operational proportion (h:SQ) of 6.5 : 1.

Two  $A_d/A_r$  were evaluated based on the golden ratio proportion (Figure 1B). The partition baffle moved forward or backward to provide two working combinations. Firstly, riser and downcomer presented SQ of  $0.00618 \text{ m}^2$  and  $0.00382 \text{ m}^2$  ( $A_r/A_d^{1.618}$ ), respectively. Secondly, riser and downcomer presented SQ of  $0.00382 \text{ m}^2$  and  $0.00618 \text{ m}^2$  ( $A_d/A_r^{1.618}$ ), respectively.

### **Determination of hydrodynamic parameters**

All the tests carried out at a constant temperature of  $25 \pm 2 \text{ }^\circ\text{C}$  and  $750 \pm 6 \text{ mmHg}$ .

#### **Bulk liquids**

NuT ( $\mu = 0.89 \text{ mPa.S @ } 25 \text{ }^\circ\text{C}$ ) was used as Newtonian fluid. To mimic non-Newtonian conditions, CMC (Madhu Hydrocolloids Pvt. Ltd., India) was used at final concentrations of 0.10% ( $\mu = 3.00 \text{ mPa.S @ } 25 \text{ }^\circ\text{C}$ ), 0.25% ( $\mu = 7.50 \text{ mPa.S @ } 25 \text{ }^\circ\text{C}$ ) and 0.50% ( $\mu = 15.00 \text{ mPa.S @ } 25 \text{ }^\circ\text{C}$ ). CMC solutions were prepared with NuT and their final pH were corrected to 7.0.

#### **Airflow regimens**

The SRILAB operated at five different airflow regimens: 0.50 vvm ( $0.006 \text{ m}^3 \cdot \text{min}^{-1}$ ), 0.75 vvm ( $0.009 \text{ m}^3 \cdot \text{min}^{-1}$ ), 1.00 vvm ( $0.012 \text{ m}^3 \cdot \text{min}^{-1}$ ), 1.25 vvm ( $0.015 \text{ m}^3 \cdot \text{min}^{-1}$ ), and 1.50 vvm ( $0.018 \text{ m}^3 \cdot \text{min}^{-1}$ ). Oil-free compressed air was the gas phase for all experiments.

#### **Linear gas velocity ( $U_g$ )**

This was determined by dividing the volumetric airflow ( $\text{m}^3 \cdot \text{min}^{-1}$ ) by the cross-section area of the riser ( $\text{m}^2$ ).

#### **Linear velocity of the liquid ( $U_L$ )**

The SRILAB was filled up to the working volume ( $0.012 \text{ m}^3$ ) with NuT. The pH values were measured by positioning the electrode tip 0.01 m bellow the liquid surface

in the riser section (Figure 1C). They were adjusted to approximately 7.00 using 1 M HCl. Air was supplied into the system at set airflow rates (see above) for 30 s. Two millilitre aliquots of 1 M HCl were carefully added in the downcomer section, 0.01 m bellow the baffle top. The mixtures were monitored by measuring the pH variations using data acquisition at one-second intervals. When pH dropped, the time interval was considered as the  $U_L$ . In contrast to other authors,<sup>13,14</sup> no wave-like tracer oscillations were detected in this work, but only a pattern of continuous pH drop; therefore, the alternative criteria proposed by others were used.<sup>15</sup>

#### **Mixing time ( $t_M$ )**

The pH drops were followed until variations became lower than 10%, when data collections were stopped. For sequential tests (not more than three repetitions for a same bulk liquid load), the pH was always adjusted to approximately 7.00 using 1 M NaOH. After achieving the desired pH, the volume was maintained constant removing excesses of liquid.

#### **~~Global gas retention~~ Gas holdup ( $\epsilon_G$ )**

A pipe tubing manometer was built using 10 mm “speedfit pipe” and “L-elbow” connections acquired in a local hardware supplier. For measurements, a 50 mL plastic pipette was adapted after its tip had been removed (Figure 1D). The reactor was filled with NuT/CMC solutions up to the working volume and the manometer was placed in the riser section **avoiding bubble entrance**. The bulk liquid was aspirated with a pump of an aneroid sphygmomanometer. After stabilization, initial volumes were recorded ( $V_i$ ). Air was supplied into the system at set airflow rates (see above). Final volumes ( $V_f$ ) were recorded after 30 s. Using the equation 1 it was possible to establish the gas **holdup** for each treatment.

$$\epsilon_G = \frac{V_i}{V_i + V_f} \quad \text{Eq. 1}$$

#### **~~Liquid pressure~~ ( $P_L$ )**

Oscillations in bulk liquid level were converted into linear height and using the equation 2 it was possible to establish the pressure on the top after 30 s of air supply.

$$P_L = \rho_L \cdot h \cdot g \quad \text{Eq. 2}$$

Here,  $p$  represents pressure (Pa),  $\rho_m$  represents the liquid density ( $1000 \text{ kg}\cdot\text{m}^{-3}$ ),  $h$  represents height (m), and  $g$  is acceleration due to gravity ( $9.81 \text{ m}\cdot\text{s}^{-2}$ ).

## Volumetric oxygen transfer coefficient ( $k_La$ )

The SRILAB was filled up to the working volume with either NuT or CMC solutions. pH was adjusted to approximately 7.00 using 1 M HCl. Nitrogen 5.0 was sparged into the system at a flow rate of  $0.012 \text{ m}^3\cdot\text{min}^{-1}$  using a three-way needle valve system (Figure 1E). The drop in the dissolved oxygen concentration was measured using a DO-5509 oxygen meter (Lutron Electron. Enterp. Co. Ltd, Taiwan). After stripping the liquid of dissolved oxygen ( $\leq 0.3 \text{ mg}\cdot\text{L}^{-1}$ ), the nitrogen valve was closed and air was supplied at set flow rates (see above) and the DO concentrations were measured until reach saturation steady state (normally,  $\sim 8.1 \times 10^{-3} \text{ kg}\cdot\text{m}^{-3}$ ). The increase in DO concentration was plotted against time (per second). Equation 2 was used to establish the different  $k_La$  values.

$$\ln(C^* - C_L) = -k_La \quad \text{Eq. 2}$$

In equation 3,  $k_L$  is the oxygen transfer coefficient ( $\text{m}\cdot\text{s}^{-1}$ );  $a$  is the gas/liquid interface area ( $\text{m}^2\cdot\text{m}^{-3}$ );  $k_La$  represents the overall oxygen transfer coefficient ( $\text{s}^{-1}$ );  $C^*$  represents the concentration of oxygen at saturation ( $\text{kg}\cdot\text{m}^{-3}$ ) that is approximately  $8.1 \times 10^{-3} \text{ kg}\cdot\text{m}^{-3}$  at  $25^\circ\text{C}$  and 1 atm;  $C_L$  is the actual dissolved oxygen concentration measured at regular intervals ( $\text{kg}\cdot\text{m}^{-3}$ ). It should be noted that mass transfer experiments assume a constant  $k_La$  value in the whole reactor.

## RESULTS AND DISCUSSION

### General considerations

1 A rectangular-split architecture was used in this study due to its superior versatility  
2 and better performance characteristics for a given oxygen transfer rate.<sup>16</sup> In addition,  
3 industrial-sized rectangular reactors are usually easier to build and to maintain than  
4 cylindrical ones.<sup>4,17</sup>

5 Although they have some disadvantages related to the presence of possible dead  
6 zones, their geometry facilitates servicing and gives unlimited number of ratios between  
7 aerated and non-aerated compartments,<sup>7</sup> which are important for future improvements  
8 in performance. Finally, the rectangular-split architecture allows the accommodation of  
9 scaffolds for biofilms, which can be mounted, removed or replaced in straightforward  
10 manner.

11 Microbial suspensions may at times behave as pseudoplastic and present a non-  
12 Newtonian behaviour,<sup>18</sup> mainly when they present extracellular polysaccharides. To  
13 mimic non-Newtonian conditions, CMC was used at different concentrations. CMC  
14 solutions can model various types of non-Newtonian fluids used in many industrial  
15 processes due to their shear-thinning property<sup>19</sup> and to their ability to mimic sludge,<sup>20</sup> as  
16 well as fungal cultures.<sup>21</sup>

17 In the experiments for calculation of  $k_L a$ , the gas and liquid phases were assumed  
18 as perfectly mixed and any oxygen concentration changes in the gas phase were  
19 disregarded.

## 20 **Hydrodynamic parameters**

21 Fifteen repetitions of each hydrodynamic test were performed and all data were  
22 plotted in MS-Excel® 2016 (Microsoft Co, Redmond, WA) spreadsheets. Statistical  
23 analyses were performed within SPSS 22.0 (IBM Co, Armonk, NY) using Kolmogorov-  
24 Smirnov test. Multiple comparisons were made using Tukey test at a significance level  
25 of 0.05. Table 1 shows the average and standard deviation values for all hydrodynamic  
26 tests assayed. For each parameter, comparisons of performance in a same fluid for  
27 different airflow ( $U_G$ ) were performed. It is noticeable that most of the values of



measured/calculated variables tend to increase as a function of increments in airflow ( $U_G$ ) for both  $A_r/A_r^{1.618}$  and  $A_d/A_r^{1.618}$ . In some cases, however, such increments were not linear or even and oscillated significantly. In the case of  $t_M$ , in particular, the values drop as a function of  $U_G$ , not following the above statement. To assess the statistical significance of the differences in terms of cross-section dimensions, Student's  $t$  test was employed at a significance level of 0.05.

When  $U_G$  has been set as a fixed parameter, all variables analysed showed a tendency of grouping in line with their  $A_r/A_d$  and  $A_d/A_r$  architecture. Figure 2 (A to C) demonstrate this and the higher degree of homogeneity for data from  $A_d/A_r^{1.618}$ . However, it is possible to notice that despite the higher dispersion of data,  $A_r/A_d^{1.618}$  promoted desirable overall increments in hydrodynamic parameters, as previously predicted.<sup>13</sup>

Variations of  $\varepsilon_G$  with  $U_G$  are shown in Figure 2A for the various CMC solutions. The figure reveals a linear development of resulting curves, contrary to observations by other authors,<sup>15</sup> who reported the existence of three different flow regimes for viscous solutions in split-cylinder airlift bioreactor. Such disparity between our results and those of Molina et al.<sup>15</sup> are likely because although both studies used viscous solutions, they applied lower  $U_G$  set points than those used by us. In addition, they used sucrose generating viscous Newtonian fluids, while CMC solutions are non-Newtonian. As stated above, CMC solutions simulate real fermentation situations.<sup>21</sup>

Conversely, the results presented here are similar to those obtained by others<sup>22</sup> with split cylinder ALB operating with  $U_G$  in a range close to those used in the current research. Overall  $\varepsilon_G$  increased approximately linearly with  $U_G$ . Such findings are interesting because linear behaviour facilitates the prediction of the fluid features in a more straightforward manner. High  $\varepsilon_G$  values may indicate that a part of the bubbles within the flow do not break at the surface and recirculate into the downcomer, increasing the mean residence time. When operating at high  $U_G$ , intensive eddy motions with high

1 local flow velocities may entrap some smaller bubbles within the dispersion for some  
2 time<sup>23</sup> ~~leading to increase in  $P_L$  (Figure 2A).~~

3 The geometry of ~~riser and downcomer~~ partition exerts a co-related influence upon  
4  $t_M$  and  $U_L$  with trend lines for different experimental groups demonstrating opposing  
5 trends for higher concentration CMC solutions, inverted for both parameters. Reduction  
6 in  $t_M$  occurs due to increased  $U_L$ ; that is why trend lines appear inverted in Figures 2B  
7 and 2C.

8 It is interesting to note that at  $A_r/A_d^{1.618}$ , solutions that are more viscous behave  
9 opposite to diluted or tap water for both parameters (no statistical analyses were carried  
10 out). On the other hand,  $A_d/A_r^{1.618}$  exerts a minor influence, regardless gas flow rate.  
11 The effect of  $U_G$  on mixing is not as significant since  $t_M$  shows a plateau (Figure 2C).  
12 Indeed, it has been already reported that higher  $U_G$  consumes more energy not  
13 necessarily improving mixing.<sup>14</sup>

14 Superficial liquid velocity and mixing time are influenced by several factors, such  
15 as  $U_G$ , viscosity/density of bulk liquid, and bioreactor geometry. In terms of the bioreactor  
16 geometry, some variables, such as the partition ratio, may interfere with the  
17 performance. For ALB operating with concentric draft tubes, risers with larger cross-  
18 section ratios promote reduction in circulation velocities; therefore gas residence times  
19 increase.<sup>14</sup> The results with SRILAB operating with  $A_r/A_d^{1.618}$  and  $A_d/A_r^{1.618}$  align with such  
20 observations (Table 1). No significant differences ( $p > 0.05$ ) were only observed when  
21 tap water was used under an airflow rate between 0.50 vvm and 0.75 vvm.

22 A reduction in mixing time can be considered desirable because nutrients can be  
23 rapidly distributed, extra-cellular metabolites can be dispersed, and heat transfer can  
24 intensify.<sup>24</sup> However, higher  $U_G$  generates turbulence and local shear stress that can  
25 damage biofilm architecture or interfere with cellular physiology.<sup>25</sup> On the other hand, if  
26  $U_L$  is low ( $< 0.01 \text{ m s}^{-1}$ ), gravitational sedimentation of solids may occur.<sup>26</sup> Since  $U_L$  values

used in these experiments were higher than the reported value, the possibility of cell deposition can be disregarded.

### Volumetric oxygen transfer

To become economically viable, aerobic fermentations require a maximum rate of oxygen transfer while minimizing the power requirements. The binomial increase of  $k_La$  and reduction of air intake should always be a goal to be achieved. Results show that larger riser cross-section area ( $A_r/A_d^{1.618}$  ratio) increases  $k_La$  values, regardless of the bulk liquid viscosity in a given pair of ratios ( $p \leq 0.018$ ) (Figure 2D). A previous study<sup>26</sup> with SRILAB of  $A_d/A_r^{1.000}$ ,  $A_d/A_r^{0.810}$ , and  $A_d/A_r^{0.650}$  had already shown that  $k_La$  increases with decreasing  $A_d/A_r$  ratio. As heterogeneous flow for  $\epsilon_G$ , caused by bubble coalescence that reduces area for mass transference and increases turbulence,<sup>27</sup> was not detected, it is assumed that the increased residence time of air bubbles ascending in a less turbulent flow in the  $A_r/A_d^{1.618}$  ratio contributed to higher  $k_La$  values. This  $A_r/A_d$  ratio is sufficiently close to  $1.650^{[26]}$  to propose that the maximum performance may be near such range. In a diverse way, it was reported previously that ALBs with rectangular geometry but without gas-liquid separator tend to achieve higher  $k_La$  with  $A_d/A_r^{2.000}$ .<sup>[7]</sup> Possibly, the presence of the gas-liquid separator expansion on the downcomer side of our SRILAB had facilitated the gas disengagement and eliminated gas stagnation in the upper portion of the bioreactor,<sup>[26,28]</sup> what can explain such differences.

As expected, viscosity influenced the  $k_La$  for a same cross-sectional area, requiring higher flow rates of air to increase values. However, in some cases,  $k_La$  increases were not significant.

Linear trendline equations derived from plotting  $k_La$  vs  $\epsilon_G$  indicated that  $A_r/A_d^{1.618}$  ratio leads to a higher oxygen transfer rate due to the longer residence time (Figure 3). Comparatively, when the larger cross-section was the riser, the equations indicated higher coefficients for each pair in a same bulk fluid. Indeed,  $A_d/A_r^{1.618}$  ratio generated even negative coefficient when NuT was used.

Exponential equations to express correlation between  $k_{La}$  and  $\epsilon_G^{29}$  were obtained after compiling all data in a same graph as continuous data and the equation (Eq. 3) is presented.

$$k_{La} = C_x \times \epsilon^n \quad \text{Eq. 3}$$

~~In such equation,  $k_{La}$  is the volumetric oxygen transfer coefficient ( $s^{-1}$ );  $C_x$  is the coefficient;  $\epsilon$  is the gas holdup;  $n$  is the exponent.~~ Resulting equations are  $k_{La} = 0.0570\epsilon_G^{0.1646}$  for  $A_r/A_d^{1.618}$  and  $k_{La} = 0.0207\epsilon_G^{-0.0170}$  for  $A_d/A_r^{1.618}$ . The  $A_r/A_d^{1.618}$  ratio definitely presented better results.

As it can be expected, the results showed that the continuous transfer of oxygen is superior when the larger cross-section is used as riser. Indeed, attempts to improve  $k_{La}$  in airlift reactors shall focus on enhancement of gas holdup.<sup>30</sup>

### Limitations

This study was limited to comparing riser and downcomer partitioning based on the golden ratio. It was not the idea to compare other architectures, once the possibilities could be enormous. Indeed, there is a consensus amongst authors that increasing SQ in riser area hydrodynamics become more favourable;<sup>13,26</sup> however, there is a lack of consensus about which  $A_d/A_r$  or  $A_r/A_d$  is more beneficial. Our modest contribution is restricted to evaluating differences between two partitioning systems based on the premise that the golden ratio may help to solve this impasse. Obviously, more data are required to establish the best combination.

Small ALBs usually can be assumed as ideally mixed tanks when operating with Newtonian liquid and high volumetric input gas flow, but scale up based on data from them can be difficult, mainly when three-phase systems are involved.<sup>31</sup> However, once fixed the conditions, hydrodynamic parameters tend to be improved in bigger ALBs. This can occur due the smaller specific friction against liquid circulation in bigger reactor scales.<sup>32</sup> The central idea of this study was to evaluate the plausibility of using golden

ratio in ALBs. Based on results obtained here, bench-to-plant scaling up studies can be designed to verify its industrial applicability.

## CONCLUSIONS

Once the same input airflow rate was established, hydrodynamic parameters were measured for two ratio conditions,  $A_r/A_d^{1.618}$  and  $A_d/A_r^{1.618}$ . The performance for the first condition was superior for  $\varepsilon_G$  and  $k_{La}$ . Values for  $t_M$  and  $U_L$  were better for the second condition.

Based on the obtained results, it is possible to conclude that SRILAB with partitioning following the golden ratio ( $A_r/A_d^{1.618}$ ) seems to be a suitable engineering solution.

~~Hydrodynamic evaluations were carried out with tap water (Newtonian fluid) and carboxymethyl cellulose (CMC) solutions at different concentrations (non-Newtonian fluid). In general, the hydrodynamic parameters were more affected by the cross-section ratio architecture than by the rheological characteristics of bulk fluids.~~

~~For biotechnological purposes, the most important feature is the ability to supply oxygen to satisfy cellular demands in a constant manner. Thus,  $k_{La}$  is the most important parameter and evaluated in the research reported here. The results observed here are in agreement with results reported previously and indicate a close relationship between  $U_G$  and  $k_{La}$ . Such relationship corroborates for better performance of  $A_r/A_d^{1.618}$  cross-section ratio.~~

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## ETHICAL APPROVAL

This article does not contain any studies with human participants or animals performed by any of the authors.

## CONFLICT OF INTEREST

The authors declare no financial or commercial conflict of interest.

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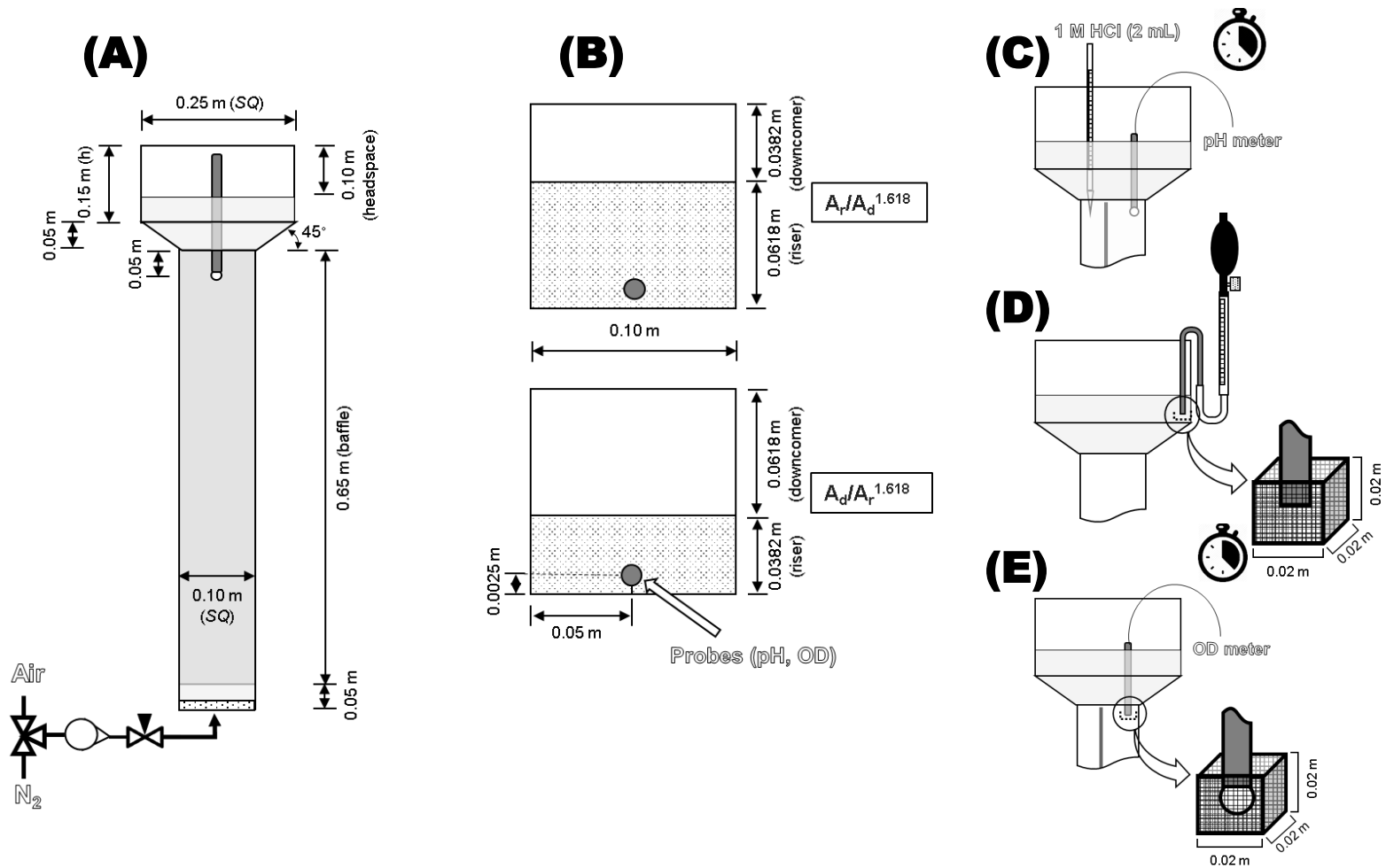


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**Table 1.** Values for different hydrodynamic and mass transfer variables.

Air flow	vvm m <sup>3</sup> min <sup>-1</sup>	0.50	0.75	1.00	1.25	1.50	Bulk
		0.006	0.009	0.012	0.015	0.018	
$\varepsilon_G$ (-)	$A_r/A_d^{1.618}$	0.112 ± 0.002 A*	0.139 ± 0.002 B*	0.165 ± 0.002 C*	0.189 ± 0.003 D*	0.213 ± 0.003 E*	NuT
	$A_d/A_r^{1.618}$	0.020 ± 0.001 A	0.038 ± 0.001 B	0.056 ± 0.001 C	0.074 ± 0.001 D	0.075 ± 0.001 D	
	$A_r/A_d^{1.618}$	0.020 ± 0.001 A*	0.038 ± 0.001 B*	0.074 ± 0.001 C*	0.107 ± 0.001 D*	0.152 ± 0.002 E*	0.10% CMC
	$A_d/A_r^{1.618}$	0.012 ± 0.001 A	0.019 ± 0.001 B	0.038 ± 0.001 C	0.056 ± 0.001 D	0.074 ± 0.001 E	
	$A_r/A_d^{1.618}$	0.091 ± 0.002 A*	0.094 ± 0.001 A*	0.107 ± 0.001 B*	0.123 ± 0.002 C*	0.153 ± 0.002 D*	0.25% CMC
	$A_d/A_r^{1.618}$	0.020 ± 0.001 A	0.030 ± 0.001 B	0.038 ± 0.001 C	0.056 ± 0.001 D	0.074 ± 0.001 E	
	$A_r/A_d^{1.618}$	0.090 ± 0.002 A*	0.107 ± 0.001 B*	0.152 ± 0.002 C*	0.166 ± 0.002 D*	0.194 ± 0.003 E*	0.50% CMC
	$A_d/A_r^{1.618}$	0.038 ± 0.002 A	0.056 ± 0.001 B	0.074 ± 0.001 C	0.091 ± 0.001 D	0.123 ± 0.002 E	
	$A_r/A_d^{1.618}$	0.199 ± 0.004 A <sup>0</sup>	0.199 ± 0.003 A <sup>0</sup>	0.133 ± 0.002 B	0.160 ± 0.002 C	0.160 ± 0.002 C	NuT
	$A_d/A_r^{1.618}$	0.199 ± 0.004 A	0.199 ± 0.003 A	0.266 ± 0.003 B*	0.266 ± 0.001 B*	0.267 ± 0.003 B*	
	$A_r/A_d^{1.618}$	0.159 ± 0.003 A	0.133 ± 0.002 B	0.114 ± 0.001 C	0.133 ± 0.002 B	0.133 ± 0.002 B	0.10% CMC
	$A_d/A_r^{1.618}$	0.199 ± 0.004 A*	0.199 ± 0.003 A*	0.266 ± 0.003 B*	0.202 ± 0.001 A*	0.267 ± 0.003 B*	
$U_L$ (m s <sup>-1</sup> )	$A_r/A_d^{1.618}$	0.080 ± 0.002 A	0.114 ± 0.002 B	0.088 ± 0.001 C	0.114 ± 0.002 D	0.133 ± 0.002 E	0.25% CMC
	$A_d/A_r^{1.618}$	0.199 ± 0.004 A*	0.199 ± 0.003 A*	0.199 ± 0.002 A*	0.204 ± 0.001 B*	0.200 ± 0.003 A*	
	$A_r/A_d^{1.618}$	0.066 ± 0.001 A	0.089 ± 0.001 B	0.079 ± 0.001 C	0.100 ± 0.001 D	0.114 ± 0.001 E	0.50% CMC
	$A_d/A_r^{1.618}$	0.159 ± 0.003 A*	0.133 ± 0.002 B*	0.199 ± 0.002 C*	0.200 ± 0.001 C*	0.200 ± 0.003 C*	
	$A_r/A_d^{1.618}$	4.186 ± 0.083 A	4.293 ± 0.058 B*	6.089 ± 0.072 C*	5.403 ± 0.073 D*	5.110 ± 0.067 E	NuT
	$A_d/A_r^{1.618}$	5.183 ± 0.103 A*	4.093 ± 0.055 B	4.093 ± 0.048 B	4.102 ± 0.055 B	5.310 ± 0.069 A*	
$t_M$ (s)	$A_r/A_d^{1.618}$	5.482 ± 0.108 A*	6.389 ± 0.086 B*	7.088 ± 0.084 C*	6.304 ± 0.085 BD*	6.212 ± 0.081 D*	0.10% CMC
	$A_d/A_r^{1.618}$	4.286 ± 0.085 A	4.991 ± 0.067 B	4.093 ± 0.048 C	4.102 ± 0.055 C	4.308 ± 0.056 D	
	$A_r/A_d^{1.618}$	10.166 ± 0.201 A*	7.388 ± 0.099 B*	9.084 ± 0.107 C*	7.204 ± 0.097 D*	6.212 ± 0.081 E*	0.25% CMC
	$A_d/A_r^{1.618}$	6.080 ± 0.120 A	6.189 ± 0.083 A	6.089 ± 0.072 A	5.203 ± 0.070 B	5.210 ± 0.068 B	
	$A_r/A_d^{1.618}$	12.060 ± 0.239 A*	9.085 ± 0.122 B*	10.083 ± 0.119 C*	8.205 ± 0.111 D*	7.414 ± 0.097 E*	0.50% CMC
	$A_d/A_r^{1.618}$	6.179 ± 0.122 A	8.286 ± 0.112 B	6.189 ± 0.073 A	6.204 ± 0.084 A	7.114 ± 0.093 C	
$k_L a$ (s <sup>-1</sup> )	$A_r/A_d^{1.618}$	0.065 ± 0.002 A*	0.069 ± 0.001 B*	0.066 ± 0.001 AB*	0.088 ± 0.001 C*	0.118 ± 0.002 D*	NuT
	$A_d/A_r^{1.618}$	0.038 ± 0.001 A	0.024 ± 0.001 B	0.023 ± 0.001 B	0.031 ± 0.001 C	0.030 ± 0.001 C	
	$A_r/A_d^{1.618}$	0.049 ± 0.001 A*	0.052 ± 0.001 B*	0.053 ± 0.001 B*	0.055 ± 0.001 C*	0.058 ± 0.001 D*	0.10% CMC
	$A_d/A_r^{1.618}$	0.028 ± 0.001 A	0.021 ± 0.001 B	0.020 ± 0.001 B	0.028 ± 0.001 A	0.028 ± 0.001 A	
	$A_r/A_d^{1.618}$	0.024 ± 0.001 A*	0.030 ± 0.001 B*	0.038 ± 0.001 C*	0.035 ± 0.001 C*	0.036 ± 0.001 C*	0.25% CMC
	$A_d/A_r^{1.618}$	0.021 ± 0.001 A	0.014 ± 0.001 B	0.019 ± 0.001 A	0.021 ± 0.001 A	0.025 ± 0.001 C	
	$A_r/A_d^{1.618}$	0.011 ± 0.001 A*	0.016 ± 0.001 B*	0.021 ± 0.001 C*	0.020 ± 0.001 C	0.032 ± 0.001 D*	0.50% CMC
	$A_d/A_r^{1.618}$	0.008 ± 0.001 A	0.014 ± 0.001 B	0.011 ± 0.001 C	0.022 ± 0.001 D <sup>0</sup>	0.023 ± 0.001 D	

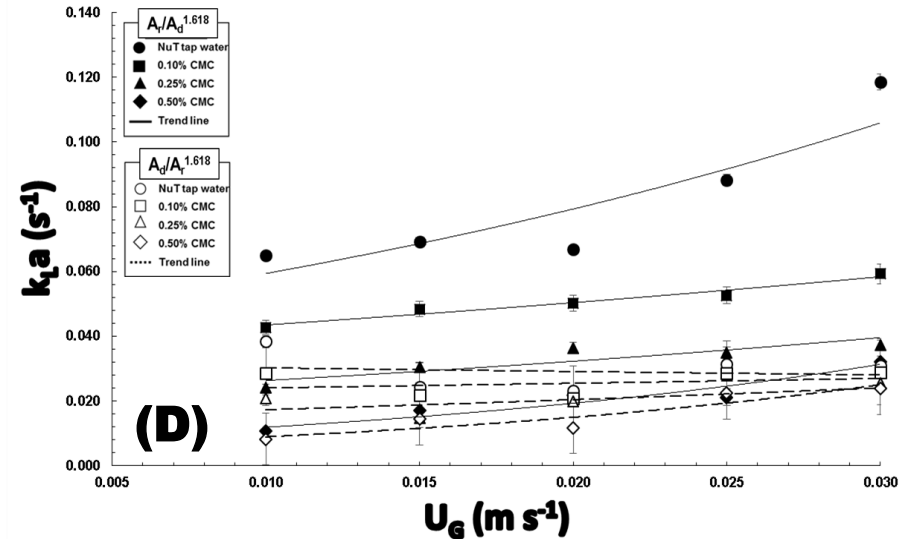
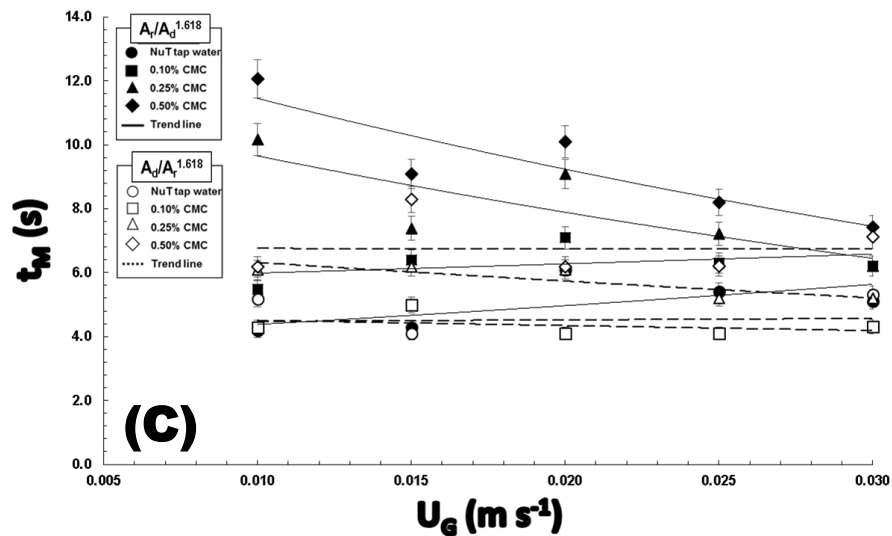
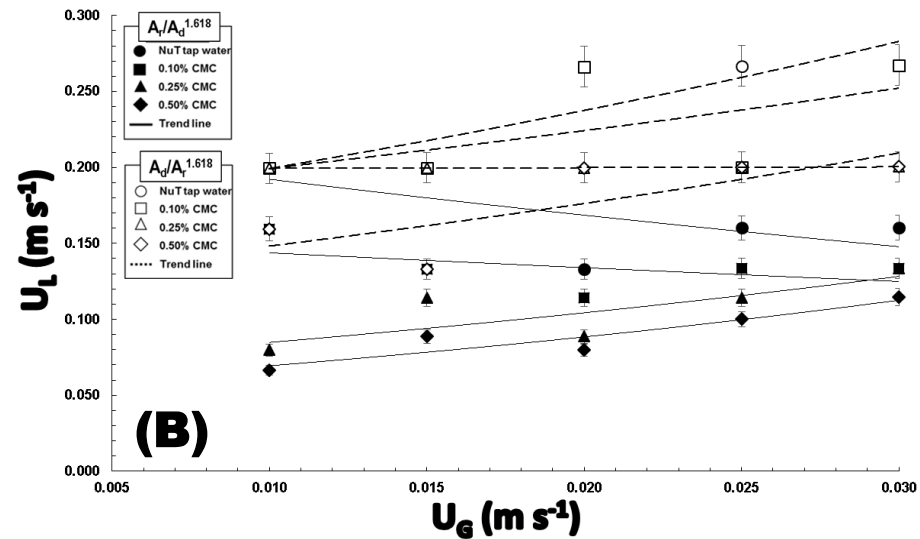
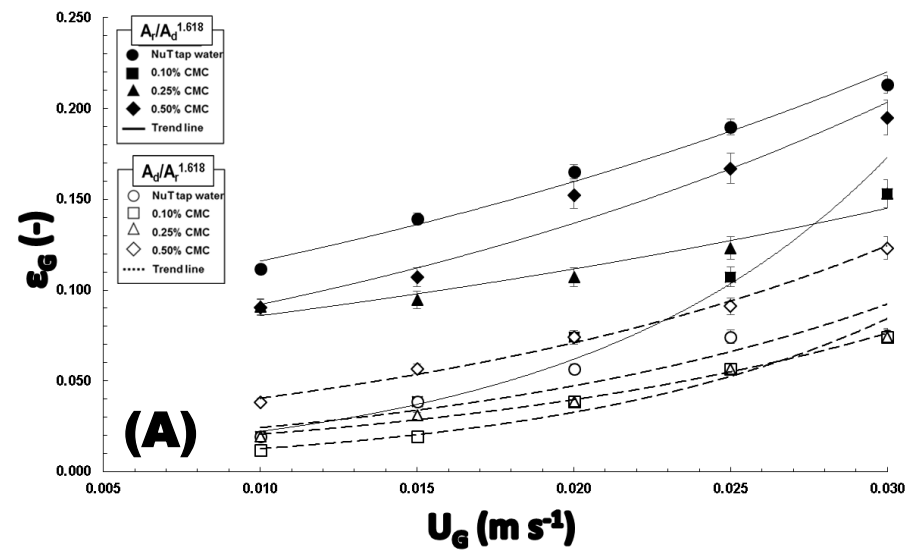
Different letters indicate differences ( $p \leq 0.05$ ) for a same row (i.e., for different airflow and  $U_G$ ). The \* signal indicates difference ( $p \leq 0.05$ ) for a given  $A_d/A_r$  pair (i.e.,  $A_r/A_d^{1.618}$  vs  $A_d/A_r^{1.618}$ ). The value harboring the \* signal is the bigger one for a given  $A_r/A_d$  or  $A_d/A_r$  pair. The number zero indicates no difference ( $p > 0.05$ ) for a given  $A_r/A_d$  or  $A_d/A_r$  pair. Symbols and abbreviations of variables in the text.



**Figure 1. Details of airlift bioreactor and hydrodynamics settings.**

**(A)** Frontal view of SRILAB. **(B)** Cross section of the column with downcomer/riser partition ratios. **(C)** Linear velocity of the liquid ( $U_L$ ) and mixing time ( $t_M$ ). **(D)** Gas holdup ( $\epsilon_g$ ). **(E)** Dissolved oxygen measurements for  $k_La$  calculations.

In (D) and (E), a cubic cell was used to avoid entrapment of air/nitrogen bubbles in probe/manometer. It was fabricated with AISI314 stainless steel ( $\phi$  0.001 m wire, mesh 0.0053 m, 70% open area). Weldings were carried out with an orthodontic spot welder.



**Figure 2. Hydrodynamic and mass transfer parameters for different architectures in airlift bioreactor operating with various air flow and Newtonian and non-Newtonian fluids. (A) Curves of  $\varepsilon_G$  as a function of  $U_G$ . (B) Curves of  $U_L$  as a function of  $U_G$ . (C) Curves of  $t_M$  as a function of  $U_G$ . (D) Curves of  $k_La$  as a function of  $U_G$ . Error bars denote standard deviations.**

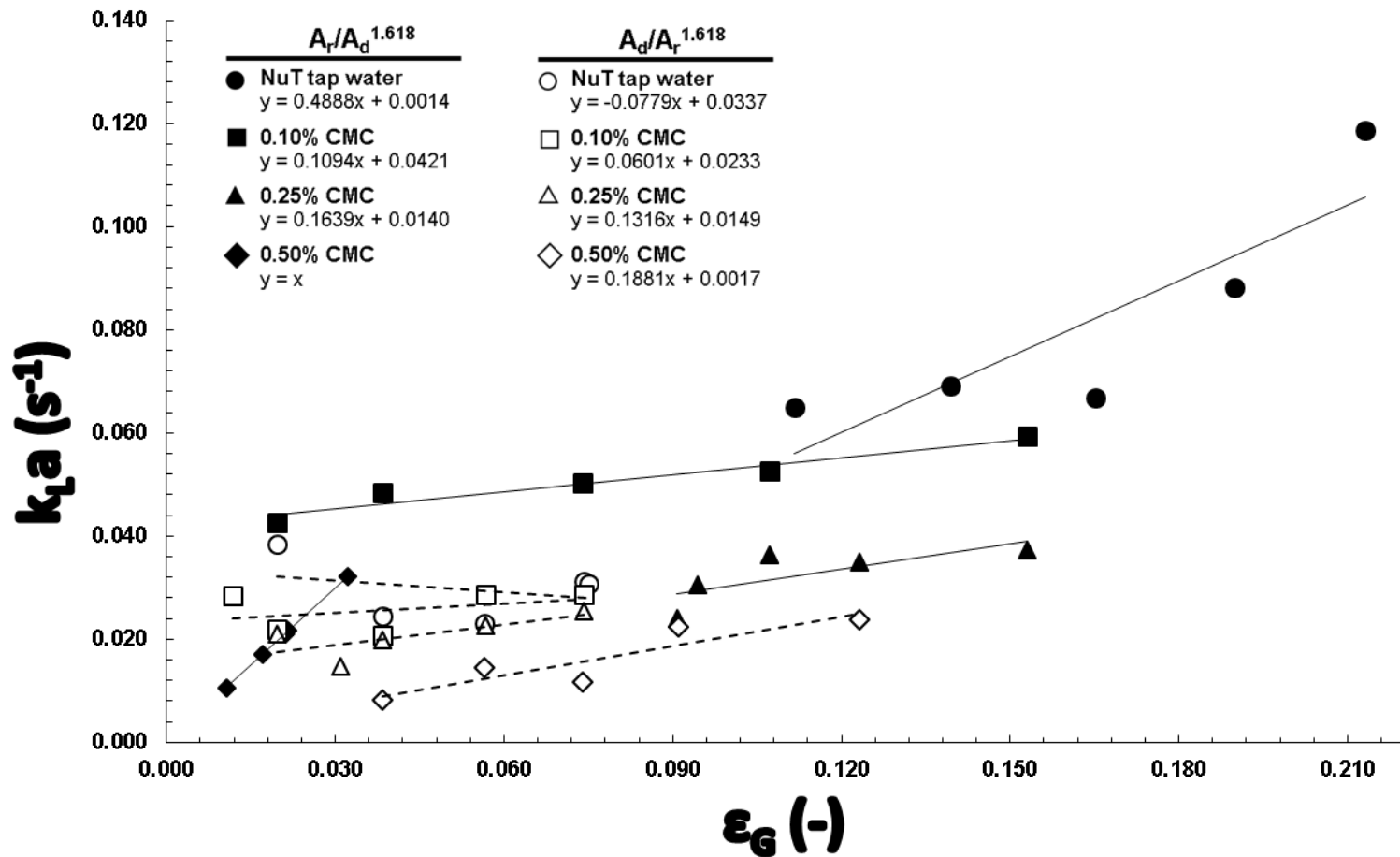


Figure 3. Linear equations derived from plotting  $k_{La}$  vs  $\epsilon_G$ .